

2. Motion in One Dimension.

→ **motion**: If the position of particle changes with time then particle will be called in motion.

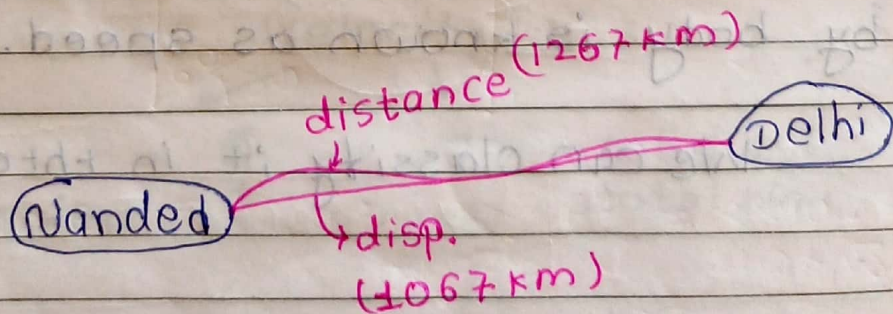
→ In given frame a body will be in motion at same time it may be at rest in another frame.

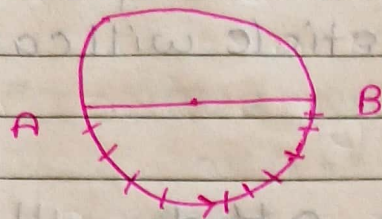
* Distance and Displacement.

→ The total length of path traced by a particle is known as distance covered by him, whereas linear distance between initial and final point is known as displacement.

→ Distance is a scalar, whereas displacement is a vector quantity.

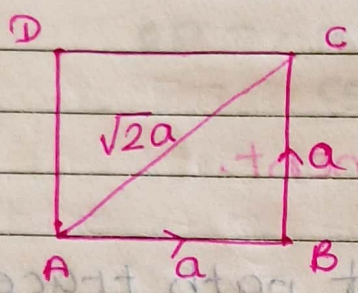
→ Unit of each is metre (m) & dimension is $[MLT^{-1}]$.





distance = πR

disp. = $2R$



distance = $2a$

disp. = $\sqrt{2} a$

* The ratio of distance & disp. is greater than or equal to 1

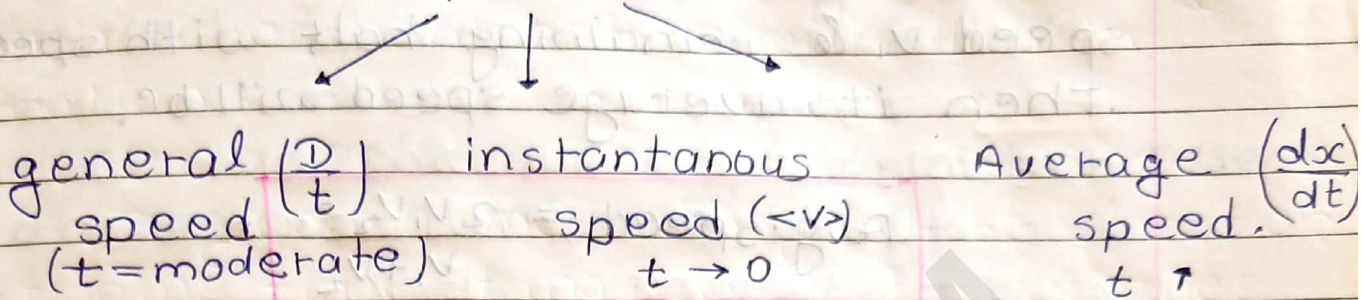
$$\frac{\text{distance}}{\text{displacement}} \geq 1$$

* Speed and velocity

The distance covered in unit time by body is known as speed.

We can classify it in three categories.

Speed

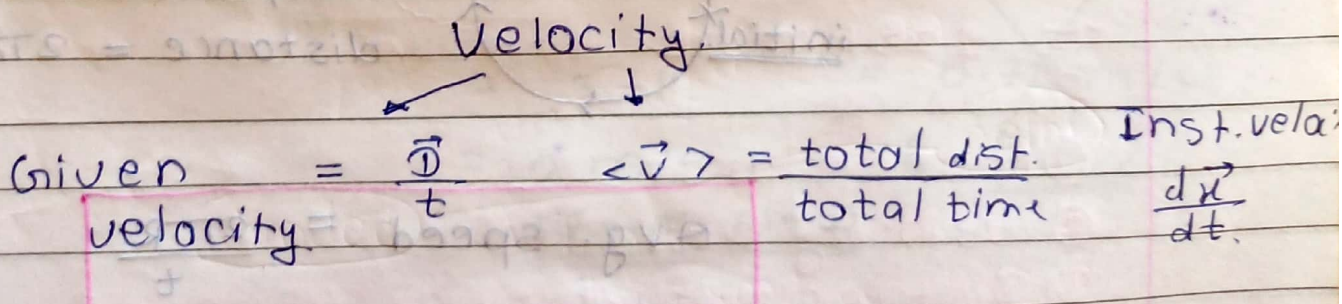


→ These classification is based upon the time interval of motion.

Speed: Speed is a scalar quantity & its unit is metre/sec. & dimension is $[m^1 L T^{-1}]$.

velocity: Vector is vector quantity. The disp. of body in unit time is known as velocity of the particle. & its unit is metre/sec. & dimension $(m^1 L T^{-1})$

On the bases of time interval we can classify it in three categories as explained below.



MTR

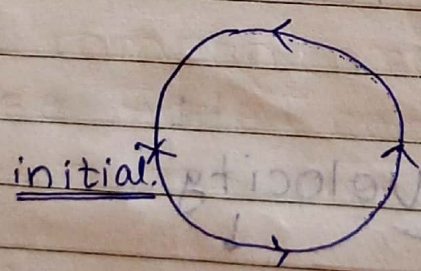
① It a car covers half distance with speed v_1 & remaining half with speed v_2 . Then its average speed will be,

$$\text{Avg. speed} = \frac{2v_1v_2}{v_1+v_2}$$

② It a car moving with speed v_1 for half time & v_2 for remaining half time the Avg. speed will be,

$$\text{Avg. speed} = \frac{v_1+v_2}{2}$$

③ In a closed path the avg. velocity is zero, but the Avg. speed is non-zero because the disp. is zero but distance is non zero,



Disp. = 0
distance = $2\pi R$

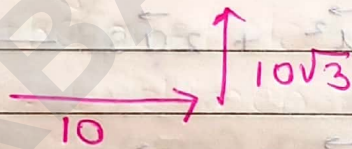
$$\text{Avg. speed} = \frac{2\pi R}{t}$$

* **Accn.** : The rate of change of velocity for a given body is known as acceleration

→ It's a vector quantity & its unit is m/sec^2 & dimension is $[MLT^{-2}]$.

→ **Calculation of accn. in different case.**

* If a car is moves toward east with $10m/s$ after $10sec$, its velocity become $10\sqrt{3}m/s$ towards north then find the accn. of car, its magnitude & its direct.



$$\frac{10\sqrt{3}j - 10i}{10}$$

$$a = \frac{10\sqrt{3}j - 10i}{10} = \sqrt{3}j - 1i = 1.73 - 1$$

$$= 3 - 1$$

$$= 0.73 \text{ am/s}^2$$

$$= 2 \text{ m/s} \quad \& \quad \underline{\underline{N-W}}$$

$$\underline{\underline{N-W}}$$

Newton's eqⁿ of motion:

To describe the motion of a particle which is moving with constant velocity & accn. which are known as eqⁿ of Newton's motion.

These eqⁿ are valid only for constant acceleration, & they are respectively as under.

$$\textcircled{1} \vec{v} = \vec{u} + \vec{a}t \quad \text{---} \textcircled{1} \quad v-t \text{ relation.}$$

$$\textcircled{2} \vec{s} = \vec{u}t + \frac{1}{2} \vec{a}t^2 \quad \text{---} \textcircled{2} \quad \vec{s}-t \text{ relation}$$

$$\textcircled{3} \vec{v}^2 = \vec{u}^2 + 2\vec{a}s \quad \text{---} \textcircled{3} \quad v/s \text{ relation.}$$

$$\textcircled{4} S_{nth} = \vec{u} + \frac{1}{2} \vec{a}(2n-1) \quad \text{---} \textcircled{4}$$

A car company Maruti blames that its deluxe model can attain velocity of 108 km/hr. just in 6 sec. the find following.

- ① accn of a car
- ② velocity after 3 sec
- ③ Distance travelled by car in 4 sec
- ④ velocity of a car after 100 m.
- ⑤ distance covered in 4th sec

① $10.8 \times \frac{5}{18} \times 5$
 $= 30 \text{ m/s}$

$v = u + at$
 $30 = 0 + a(6)$
 $a = 5 \text{ m/s}^2$

② $v = 0 + 5 \times 3$
 $v = 15 \text{ m/s}$

③ $s = \frac{1}{2} (18) \cdot 8$
 $= 72 \text{ m} = 40 \text{ m}$

④ $v^2 = 2(5)(50)$
 $v^2 = 500$
 $v = \sqrt{500}$
 $v = 10\sqrt{5} \text{ m/s}$

⑤ $s = \frac{1}{2} g (2t - 1)$

$= \frac{1}{2} (7) \times 5$

$= \frac{35}{2}$

$s = 17.5 \text{ m}$

It the velocity of an object decrease with time then the value of accn is -ve. which is also known as retardation.

In these case the eqⁿ of motion are as under:-

$$\bar{a} < 0.$$

$$v = u - at$$

$$s = ut - \frac{1}{2} at^2$$

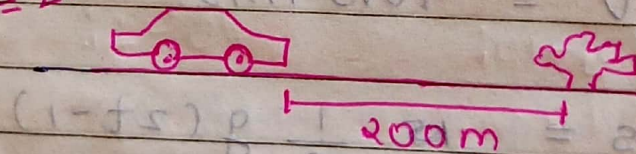
$$v^2 = u^2 - 2as$$

$$s = u - \frac{1}{2} a(2t - 1)$$

MTR 3

Stopping Distance:

$a = 2 \text{ ms}^{-2}$ 72 km/hr



$$s = \frac{u^2}{2a}$$

$$= \frac{72 \times 5}{18} = 20 \text{ m/s}$$

$$= \frac{10 \times 10}{20 \times 20} = 2 \times 2$$

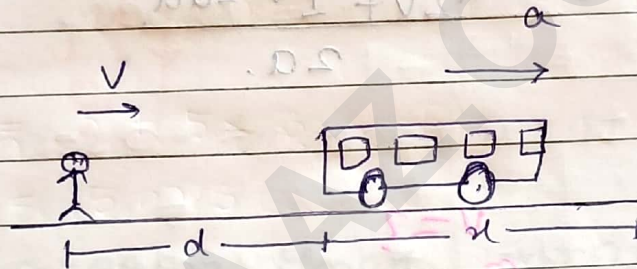
$$= 100 \text{ m}$$

$$t = \frac{v}{a}$$

$$= \frac{20}{2}$$

$$t = 10 \text{ sec.}$$

Space-gap problems :



let the person catches the bus after time t in these time let the bus travel distance s then in the same time interval man has to catch the bus

$$s = \frac{1}{2} a t^2$$

$$s + d = v t$$

$$\frac{1}{2} a t^2 + d = v t$$

$$a t^2 + 2d - 2v t = 0$$

$$a t^2 - 2v t + 2d = 0$$

$$b^2 - 4ac = 4v^2 - 4a^2d$$

$$= 4v^2 - 8ad.$$

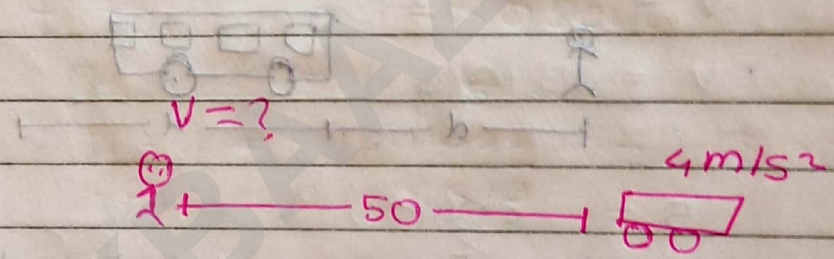
MTR = 4

$$v = \frac{2 \cdot 8ad}{4}$$

$$v \geq \sqrt{2ad}$$

$$t = \frac{2v \pm \sqrt{2ad}}{2a}$$

#

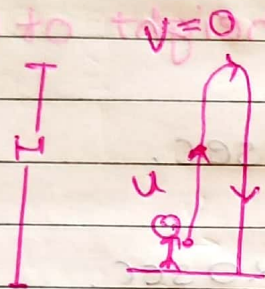


$$v = \sqrt{2 \times 4 \times 50}$$

$$= \sqrt{400} = 20 \text{ m/s}$$

Motion under gravity

If a body is thrown vertically upwards, then its eqⁿ of motion can be written as under:



* Time to reach H_{max} * Total time

$$v = u + at$$

$$0 = u + at$$

$$\therefore t = \frac{u}{a}$$

$$t = \frac{2u}{a}$$

* H_{max} .

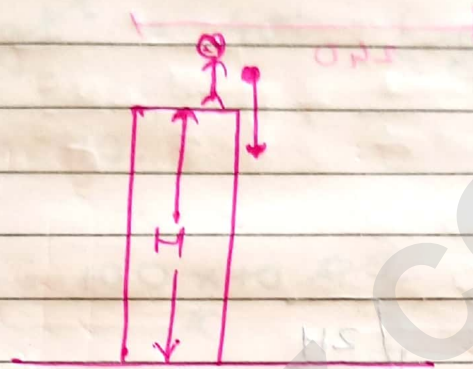
$$v^2 = u^2 + 2as$$

$$0 = u^2 + 2as$$

$$\therefore s = \frac{-u^2}{2a}$$

MTR: 5 If a body is thrown vertically upwards then for any velocity the distance covered in last is always same & it is 5 meters.

Downward projection: If a body is thrown from the top of a tower with initial velocity u in downward direction then its eqⁿ of motion are as under.



- ① $v = u + gt$,
- ② $h = ut + \frac{1}{2}gt^2$
- ③ $v^2 = u^2 + 2gs$,
- ④ $H_n = u + \frac{g}{2}(2n-1)$

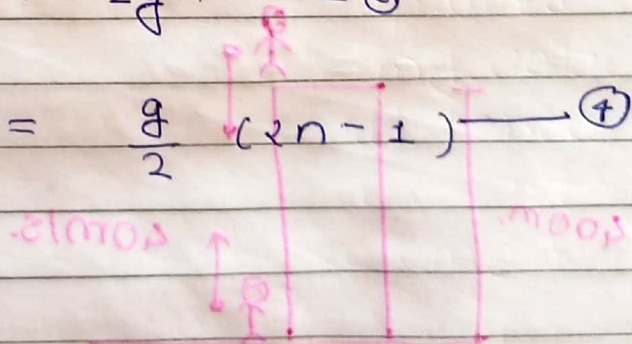
If a body is dropped from height then its initial velocity is zero then the eqⁿ of motion.

$$v = gt \quad \text{--- ①}$$

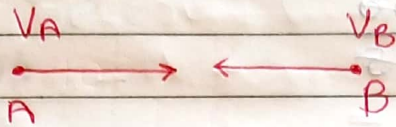
$$h = \frac{1}{2}gt^2 \quad \text{--- ②}$$

$$v^2 = 2gh \quad \text{--- ③}$$

$$h_n = \frac{g}{2}(2n-1) \quad \text{--- ④}$$



When two particles A & B are provided and their velocities V_A and V_B are respectively. Hence the velocity of V_A w.r. B. is given by following expression.

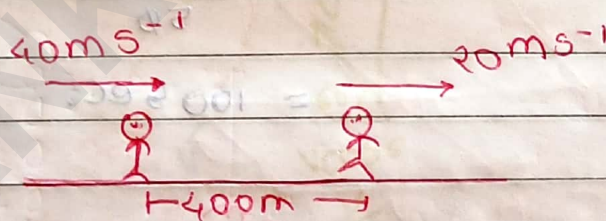


$$\vec{V}_{A/B} = \vec{V}_A + \vec{V}_B$$

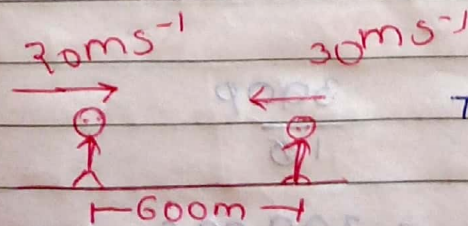


$$\vec{V}_{A/B} = \vec{V}_A - \vec{V}_B$$

①



$$T = \frac{400}{40 - 20} = \frac{400}{20} = 20 \text{ sec}$$

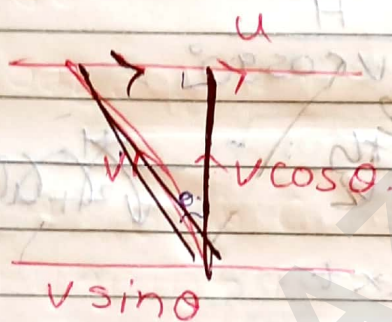


$$T = \frac{600}{50} = 12 \text{ sec}$$

River Concept

★ For shortest distance

Let a river is flowing with velocity v & a body who can swim with velocity v , in a water who wants to cross a river, we can cross it in two ways.

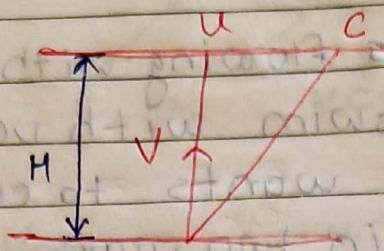


$$v \sin \theta = u$$

$$\therefore \sin \theta = \frac{u}{v}$$

$$\text{Time} = \frac{H}{v \cos \theta} = \frac{H}{\sqrt{v^2 - u^2}}$$

* For shortest time.



$$\theta = 90^\circ$$

$$t = \frac{H}{v \cos 90^\circ}$$

$$t = \frac{H}{v}$$

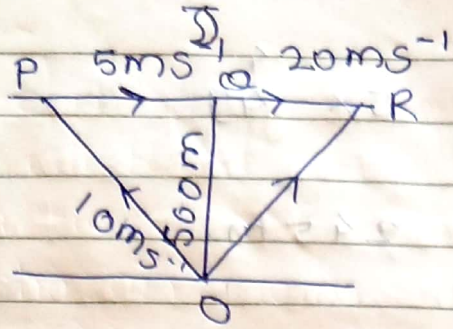
$$x = u \times t$$

$$= u \times \frac{H}{v}$$

$$= \frac{u \times H}{v}$$

There is village named and river is flowing through it two children. Kitchup & chotta many can swim in still water with speed 10 ms^{-1} . Kitchup obtained for shortest path where as manu. obtained for minimum time. If there is a mango tree in opposite side then find the time taken by them to reach the mango tree. Hence tell who will eat the 1st mango, if chatta many can run 20 ms^{-1} for the

Ans:



$$\text{Time} = \frac{H}{\sqrt{v^2 - u^2}}$$

$$= \frac{500}{\sqrt{100 - 25}}$$

$$= \frac{500}{\sqrt{75}}$$

$$= \frac{100}{5\sqrt{3}}$$

$$= \frac{100}{1.73}$$

$$= 57.80 \text{ s}$$

$$\text{Time} = \frac{H}{\sqrt{v^2 + u^2}}$$

$$= \frac{500}{\sqrt{100 + 25}}$$

$$= \frac{500}{\sqrt{125}} = \frac{57.9 \cdot 100}{50\sqrt{5}}$$

$$= 49.$$

$$\text{distance} = 5 \times 49$$

$$= 245 \text{ m.}$$

$$\text{Time} = \frac{245}{20} = 12.2$$

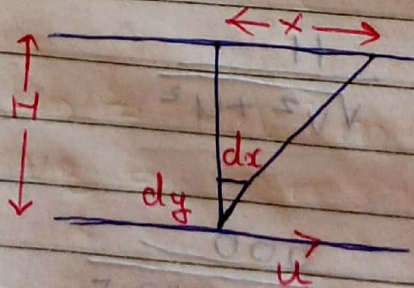
$$= 12.2 \text{ sec}$$

$$\text{Time for ketchup} = 57.80 \text{ sec}$$

$$\text{Time for mango} = 48 + 12.2 = 60.2$$

\therefore The ketchup will reach 1st & eat mango.

★ If there is a variation in a river flow and we want to calculate time of crossing then for these purpose we will use the integration method as explained the below:



Ans:

$$t = \frac{H}{u}$$

$$v \propto y$$

$$v = ky$$

$$dx = v \cdot dt$$

$$\int_0^x dx = \int_0^H \frac{ky}{u} dy$$

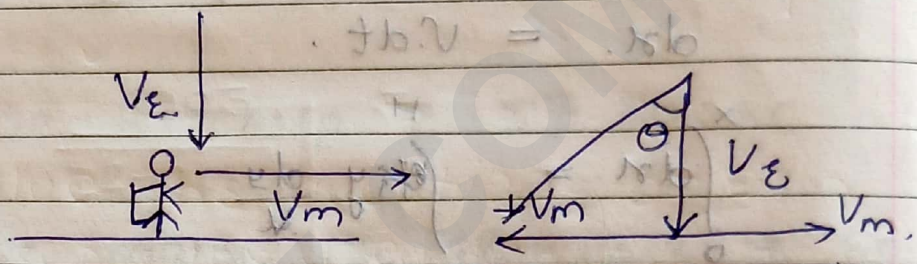
$$x = \frac{k}{u} \int_0^H y \cdot dy$$

$$x = \frac{k}{u} \frac{H^2}{2}$$

$$x = \frac{kH^2}{2u}$$

Q One day little jony was going to his school suddenly the rain start with velocity 10ms^{-1} then find the apperant speed of rain hense its direction as experianced by jony. $V_m = 10\sqrt{3}\text{ms}^{-1}$

Ans.



$$\vec{V}_{E/m} = \vec{V}_E - \vec{V}_m$$

$$\vec{V}_{E/m} = \vec{V}_E + (-\vec{V}_m)$$

① Apperant speed = $V_{E/m} = \sqrt{V_E^2 + V_m^2}$

② Direction = $\tan\theta = \frac{V_m}{V_E}$

Q. Ans :

$$V_m = 10\sqrt{3}\text{ms}^{-1}$$

$$V_E = 10\text{ms}^{-1}$$

$$|V_{E/m}| = \sqrt{100 \times 3 + 100}$$

$$= \sqrt{400}$$

$$|V_{E/m}| = 20\text{ms}^{-1}$$

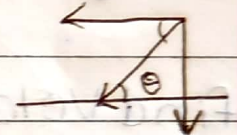
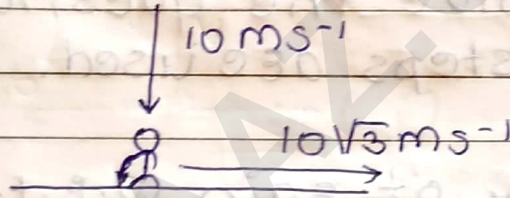
$$\tan \theta = \frac{V_m}{V_e} = \frac{10\sqrt{3}}{10} =$$

$$\tan \theta = \sqrt{3}$$

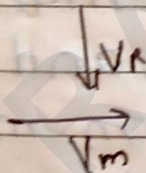
$$\theta = \tan^{-1} 60^\circ$$

For a given case find the apparent speed of rain (i) $V_{e/m}$ (ii) Direction of diff' umbrella to protect.

Ans:



$$V_{r/m} = V_r - V_m \quad |V_{e/m}| = \sqrt{100 + 100 \times 3} \quad V_{r/m} = 20 \text{ ms}^{-1}$$



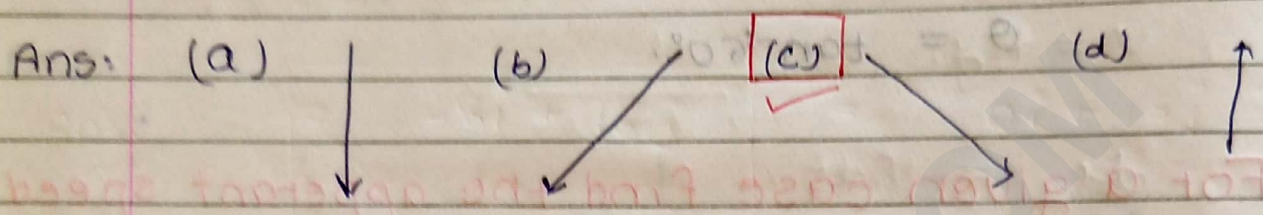
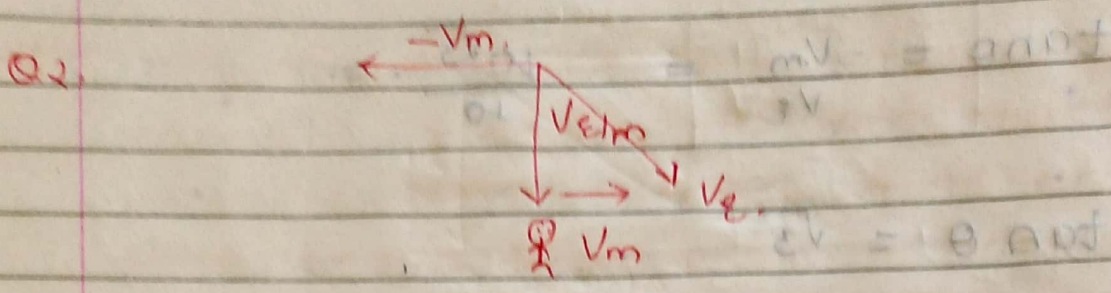
$$\tan \theta = \frac{V_e}{V_m} = \frac{10}{10\sqrt{3}}$$

V_m

$$\tan \theta = \frac{1}{\sqrt{3}}$$

$$\theta = 30^\circ$$

\therefore he had to take umbrella at 30° with horizontally.

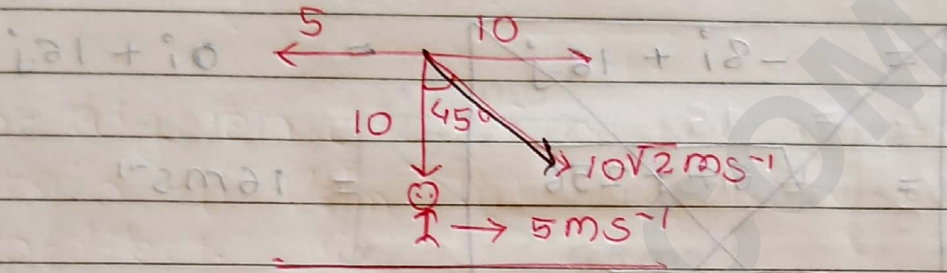


To solve the questions of rain following steps are used.

1. find Velocity of rain w.r.t. man. its magnitude will represent the speed of rain & angle will be $\theta = \tan^{-1} \frac{V_m}{V_{rain}}$
2. On increasing the speed of man apparent speed will increase and the rain will bend towards the man. more the speed man move will be the bending of rain
3. If a running man feels that rain is falling vertically downwards, then the actual direction of the ^{rain} ~~man~~ will be from the back side.

④ If we want to solve the question obtain in sec we must stop the man & its velocity to gain in opposite direction these way we can calculate a pperate speed & direction.

Q1

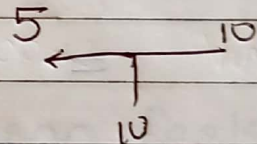


Ans:

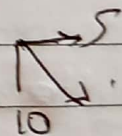
$$V_{E/m} = 5i + 10(-j)$$

$$(V_{E/m}) = \sqrt{25 + 100} = \sqrt{125} = 5\sqrt{5}$$

$$\tan \theta = \frac{5}{10}$$

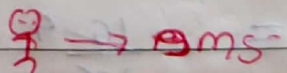
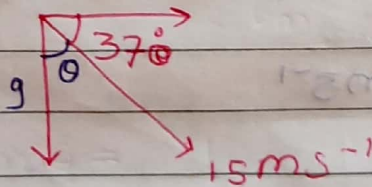


$$\theta = \tan^{-1} \frac{5}{10}$$



Q2

$$15 \times \cos 37^\circ = 12$$



Ans:

$$V_{E/m} = 9i + (9)(-j) \quad \tan \theta = \frac{9}{9} = \frac{3}{3}$$

$$= \sqrt{81 + 9}$$

$$= \sqrt{90}$$

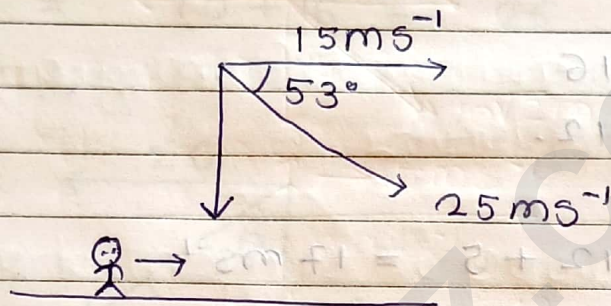
$$= 3\sqrt{10}$$

$$\tan \theta = \frac{1}{3}$$

$$\theta = \tan^{-1} \frac{1}{3}$$

If a boy standing on a road and rain is falling as shown in fig. Then find the speed of man so rain appears to him falling vertically downward?

Ans:



\therefore The boy will be move 15 m/s to appear rain vertically.

MTR

When ever a person feels that rain is falling vertically downward then the velocity of rain must be equal to horizontal component of rain.

\rightarrow To solve any question of rain & man use the following steps

(i) stops the man & give it velocity to rain in opposite direction.

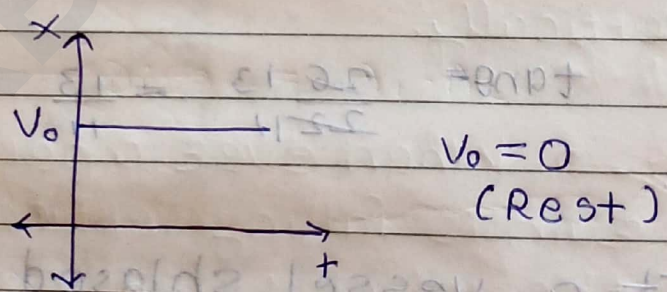
(ii) Find these relative velocity in vector form & calculate the speed

(iii) By the trigonometric write $\tan \theta$ & get the angle.

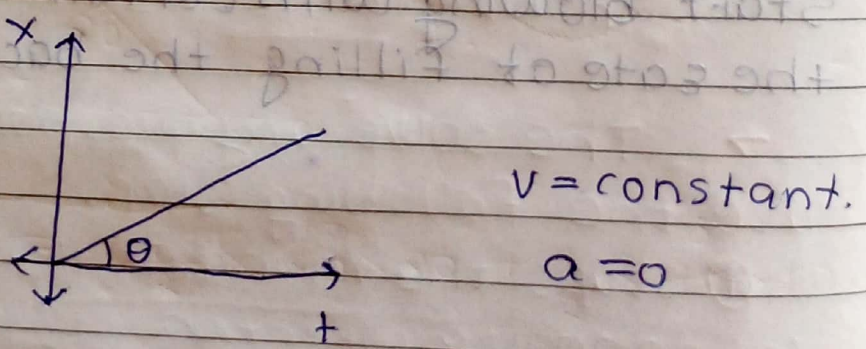
Term Analysis

1. IF the position of particle is represented with time on the graph then this is known as position time curve
2. The resultant from graph are obtained velocity.
3. The slope of tangent drawn at any point represent velocity at that point.

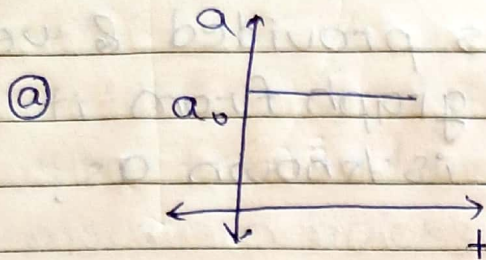
① x - t graph



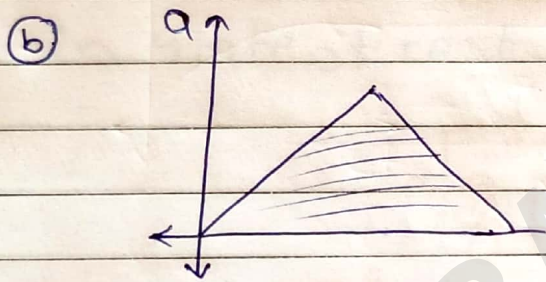
②



③ A-T curve.



acch = constant.



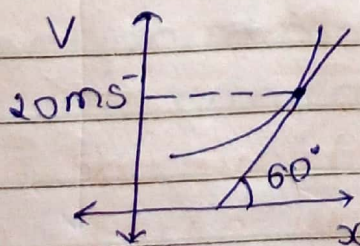
Area = change in velocity.

③

$$a = \frac{dv}{dt} \times \frac{dx}{dx}$$

$$accn = \frac{v \cdot dv}{dx}$$

④



$$a = v \cdot \frac{dv}{dx}$$

$$= 20 \times \tan 60^\circ$$

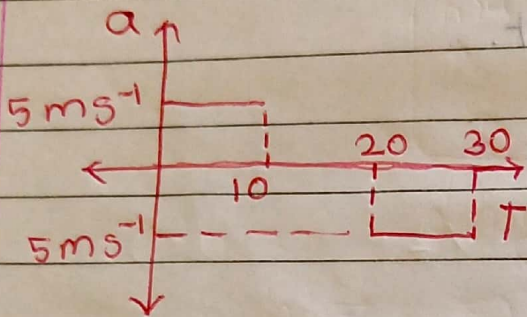
$$= 20 \times \sqrt{3}$$

change in velocity = $20\sqrt{3} \text{ ms}^{-2}$

Mutual plotting

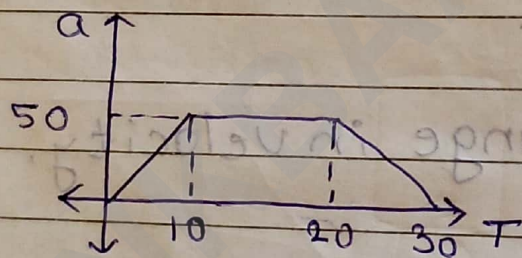
If any graph is provided & we want to plot another graph from it then these process is known as mutual plotting.

Q.

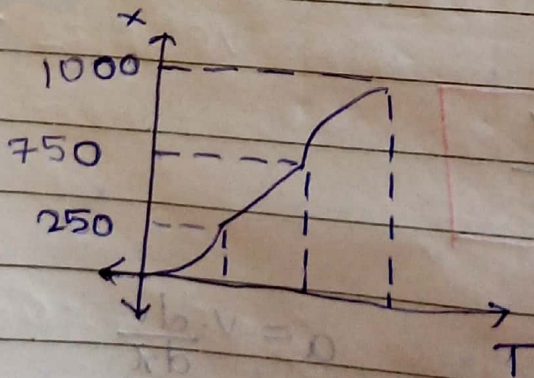


⇒

V-t.



x-t.



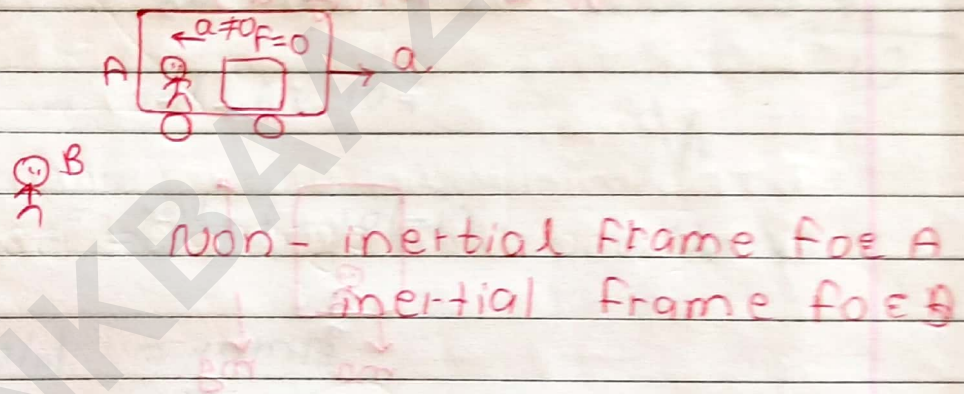
$$\frac{v_b}{x_b} = \frac{dv}{dx}$$

$$\frac{v_b}{x_b} = \frac{v}{x}$$

$$v_b v = x_b x$$

Inertia & non-inertial frame and pseudo-force

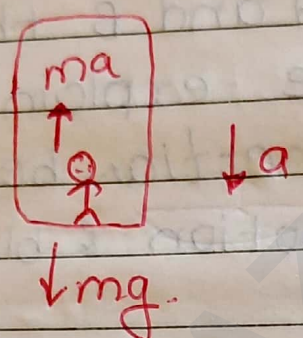
IF a body is on a moving car & the car starts suddenly then the block inside it move in backward direction. IF we consider two observers A and B then the motion of the block can be explained by A on the bases of law of inertia because he will say that car is in motion & block will continue in state of rest.



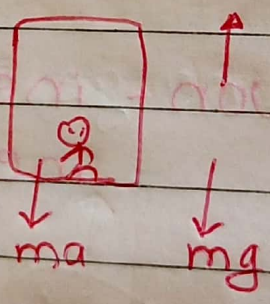
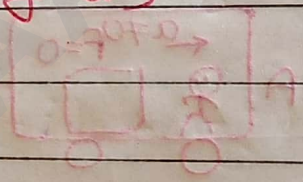
B is surprise because there is no direct force on block but accn. is non-zero which can not be prove by newton 2nd Law. $F=ma$. So to make the newtons law correct we have develop the concept of pseudoforce. means we will assume that a force will act opposite to the direction of motion of the body.

So we can conclude that "The body is inside the accelerated frame will feel the pseudo-force which is opposite to the direction of the force of the body."

So when we are moving up in a lift the pseudo force act on downward so effective weight increase. Hence lift is moving down then pseudo force will act upwards. will decrease as explain below.



$$W = m(g - a)$$

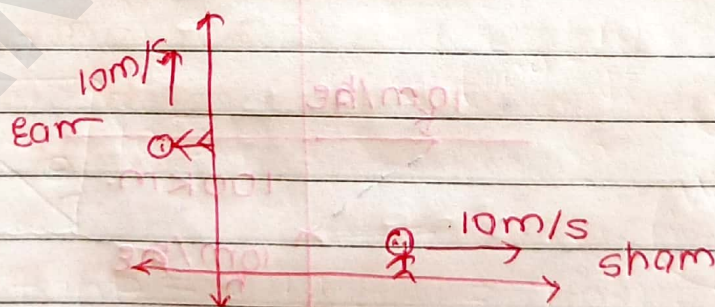


$$W = m(g + a)$$

★ Minimum Distance between two ship, cyclist.

There is a question of shortest distance between ship & cyclist then to solve such question following 4 steps are used they are as under:

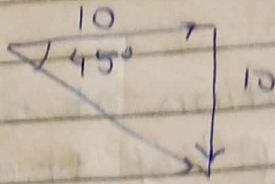
- ① Stop one of them hence gives its velocity to another one.
- ② Find the relative velocity hence draw its direction.
- ③ Draw a \perp on the these line from the body stop. the length of these \perp will represent minimum distance.
- ④ Then time taken to come to these location will be $t = \frac{d'}{V_{\text{relative}}}$



$$\vec{V}_{s/r} = V_{sh} - V_{ram}$$

$$= 10\hat{i} - 10\hat{j}$$

$$|V_{s/r}| = 10\sqrt{2} \text{ m/s}$$

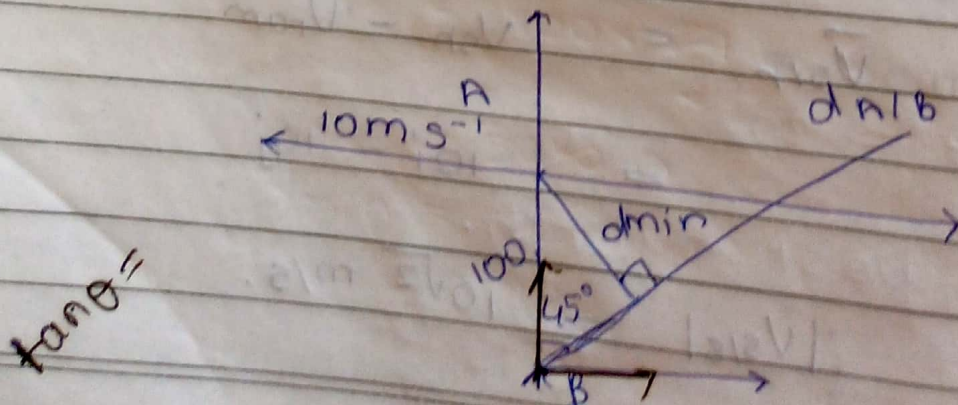
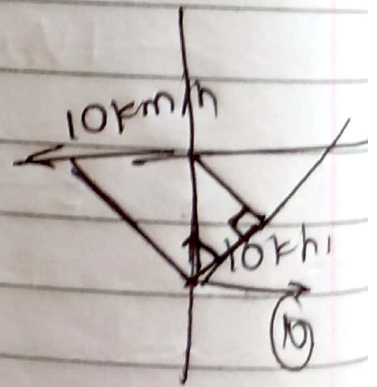
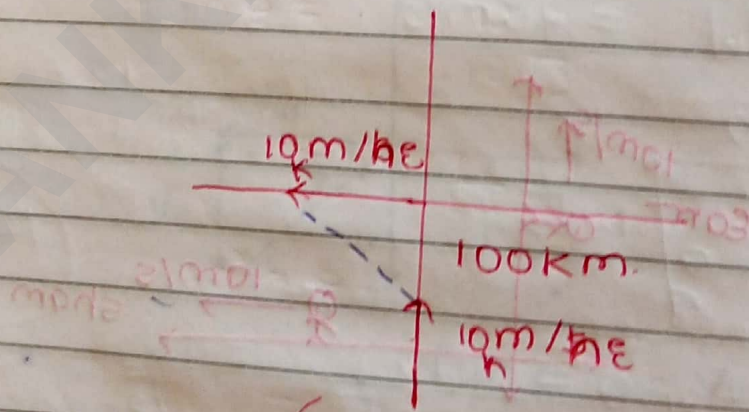


$$\theta = 45^\circ$$

S/E.

A ship is going towards west with a velocity of 10 m/s the another ship B is moving towards north, with velocity of 10 m/s if the ship B is 100 km at south from the south A then find the following.

- ① The minimum distance b/w ship A & ship B
- ② Time taken to come to these location



$$d_{\min} = 100 \sin 45^\circ$$

$$\text{dist.} = \frac{100}{\sqrt{2}}$$

$$= 50\sqrt{2} \text{ km.}$$

$$d' = d \cos 45^\circ$$

$$= 100 \times \frac{1}{\sqrt{2}}$$

$$= 50\sqrt{2} \text{ km}$$

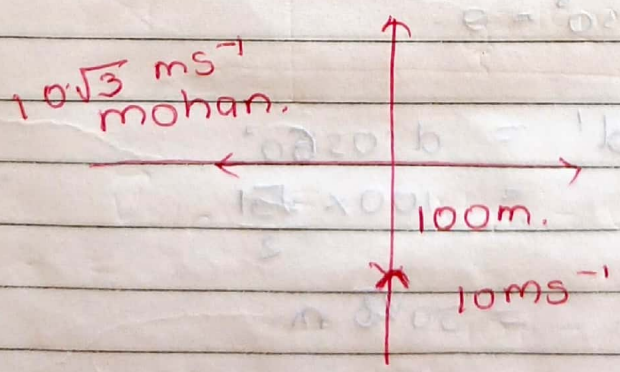
$$t = \frac{d'}{|V_{\text{rel}}|}$$

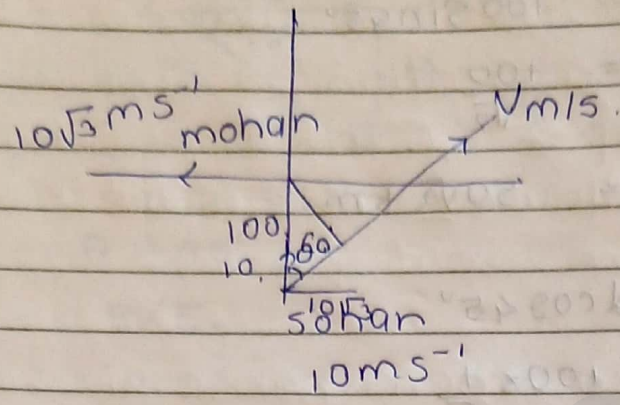
$$= \frac{50\sqrt{2}}{10\sqrt{2}}$$

Soln

$$t = 5 \text{ h}$$

* IF two cyclist mohan & soham are moving along -x & y direction resp. as shown in figure, then find the minimum distance between them.





$$\begin{aligned}
 V_{m/s} &= V_{\text{mohan}} - V_{\text{sohan}} \\
 &= 10\sqrt{3}(-i) - 10j \\
 &= 10\sqrt{3}(-i) + 10(-j) \\
 &= 20 \text{ m/s}
 \end{aligned}$$

$$\begin{aligned}
 \tan \theta &= \frac{10}{10\sqrt{3}} \\
 &= \frac{1}{\sqrt{3}}
 \end{aligned}$$

$$30^\circ = \theta$$

$$\begin{aligned}
 d' &= d \cos 60^\circ \\
 &= 100 \times \frac{1}{2} \\
 &= 50\sqrt{3} \text{ m.}
 \end{aligned}$$

$$\begin{aligned}
 d_{\text{min}} &= d \sin 30^\circ \\
 &= \frac{100}{2} \\
 &= 50\sqrt{3} \text{ m.}
 \end{aligned}$$